

Chapter 7

Correlation

Correlation

It is a statistical method or a statistical technique that measures quantitative relationship between different variables, like between price and demand. According to Croxton and Cowden, "When the relationship is of a quantitative nature, the appropriate statistical tool for discovering and measuring the relationship and expressing it in a brief formula is known as correlation."

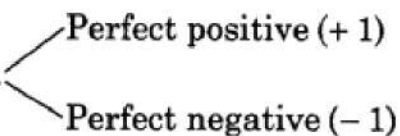
Types of Correlation

Correlation is commonly classified into negative and positive correlation.

- **Positive Correlation** When two variables move in the same direction, such a relation is called positive correlation, e.g., Relationship between price and supply
- **Negative Correlation** When two variables changes in different directions, it is called negative correlation. Relationship between price and demand.

Degree of Correlation

Degree of correlation refers to the coefficient of correlation

(i) **Perfect Correlation** 

(ii) Absence of Correlation

(iii) Limited Degree of correlation

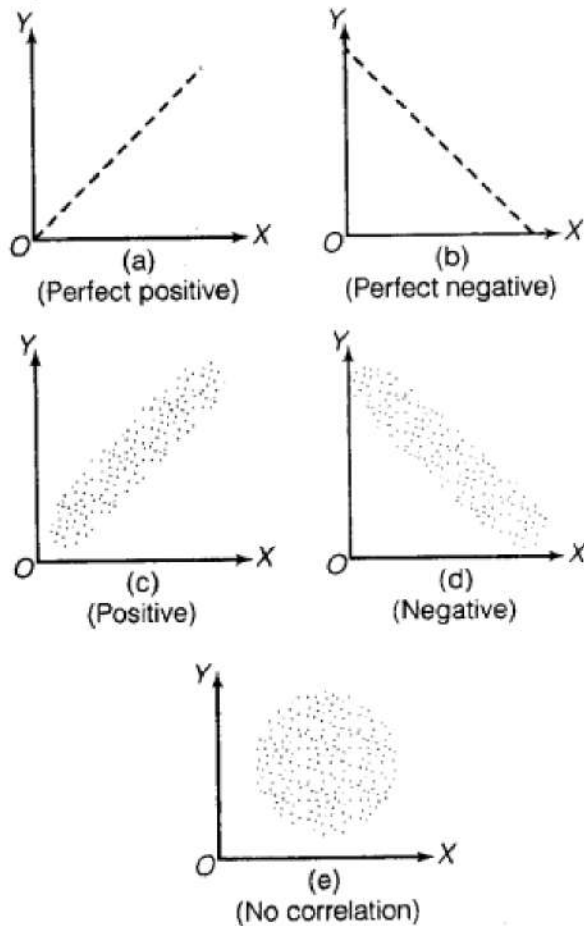
The degree of correlation between 0 and 1 may be rated as

- High (0.75 and 1)
- Moderate (0.25 and 0.75)
- Low (0 and 0.25)

Methods of Estimating Correlation



(i) Scatter Diagram Scattered diagram offers a graphic expression of the direction and degree of correlation.



Karl Pearson's Coefficient of Correlation

This is also known as product moment correlation and simple correlation coefficient.

Karl Pearson has given a quantitative method of calculating correlation. Karl Pearson's coefficient correlation is generally written as r .

Formula According to Karl Pearson's method, the coefficient of correlation is measured as

$$r = \frac{\sum xy}{\sqrt{\sum x^2 \sum y^2}}$$

Where,

r = Coefficient of correlation;

$$x = x - \bar{x}$$

$$y = y - \bar{y}$$

σ_x = Standard deviation of x series

σ_y = Standard deviation of y series

N= Number of observations

If there is no need to calculate standard deviation of x and y directly using the following formula

$$r = \frac{\sum xy}{\sqrt{\sum x^2 \sum y^2}}$$

Here, $x = (x - \bar{x})$, $y = (y - \bar{y})$

Short-cut Method

This method is used when mean value is not in whole number but in fractions. In this method, deviation is calculated by taking the assumed mean both the series. Coefficient of correlation is calculated using the following formula

$$r = \frac{\sum dxdy - \frac{(\sum dx)(\sum dy)}{N}}{\sqrt{\sum dx^2 - \frac{(\sum dx)^2}{N}} \times \sqrt{\sum dy^2 - \frac{(\sum dy)^2}{N}}}$$

Here, d_x = deviation of x series from the assumed mean = $(x - A)$

d_y = deviation of y series from the assumed mean = $(y - A)$

$\sum dxdy$ – sum of the multiple of dx and dy

$\sum dx^2$ = sum of square of dx

$\sum dy^2$ = sum of square of dy

$\sum dx$ = sum of deviation of x-series

$\sum dy$ = sum of deviation of y-series

N = Total number of items

Step Deviation Method

Coefficient of correlation is calculated using the following formula

$$r = \frac{\sum dxdy - \frac{\sum dx \sum dy}{N}}{\sqrt{\sum dx^2 - \frac{(\sum dx)^2}{N}} \sqrt{\sum dy^2 - \frac{(\sum dy)^2}{N}}}$$

Spearman's Rank Correlation Coefficient

In 1904, 'Charles Edwards Spearman' developed a formula to calculate coefficient correlation of qualitative variables. It is popularly known as Spearman's rank. Difference

formula or method.

Formula
$$r_k = 1 - \frac{6 \sum D^2}{N^3 - N}$$

Coefficient of Rank Correlation when Ranks are Equal formula

$$r_k' = 1 - \frac{6 \left[\sum D^2 + \frac{1}{12} (m_1^3 - m_1) + \frac{1}{12} (m_2^3 - m_2) + \dots \right]}{N^3 - N}$$

Here, m = number of items of equal ranks.

Importance or Significance of Correlation

- The study of correlation shows the direction and degree of relationship between the variables.
- Correlation coefficient some times suggests cause and effect relationship.
- Correlation analysis facilitates business decisions because the trend path of one variable may suggest the expected changes in the other.
- Correlation analysis also helps policy formulation.

